

## Relations & Functions

**Relation:** A mapping, or pairing, of input values with output values.

**Domain:** The set of input values.

**Range:** The set of output values.

### Representing Relations:

A relation can be represented in the following ways.

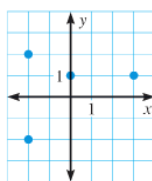
**Ordered Pairs**

$(-2, 2)$   
 $(-2, -2)$   
 $(0, 1)$   
 $(3, 1)$

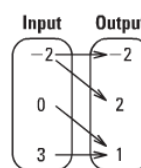
**Table**

| x  | y  |
|----|----|
| -2 | 2  |
| -2 | -2 |
| 0  | 1  |
| 3  | 1  |

**Graph**



**Mapping Diagram**



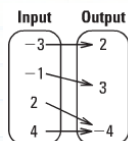
In each case the domain is  $\{-2, 0, 3\}$  and the range is  $\{-2, 2, 1\}$

Some relations are functions.

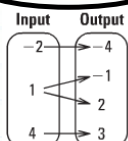
A **function** is a relation for which each input has exactly one output.

If any input of a relation has more than one output, the relation is *not* a function.

**Function**



~~Function~~

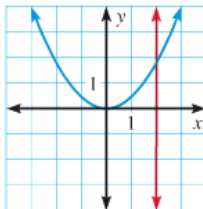


Each input must have a single output.

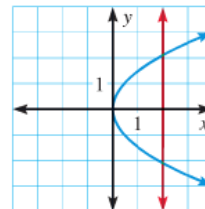
### The vertical line test:

A relation is a function if and only if no vertical line intersects the graph of the relation at more than one point.

**Function**



**Not a function**



## Equations in Two Variables

**EQUATIONS IN TWO VARIABLES** Many functions can be described by an **equation in two variables**, such as  $y = 3x - 5$ . The input variable (in this case,  $x$ ) is called the **independent variable**. The output variable (in this case,  $y$ ) is called the **dependent variable** because its value *depends* on the value of the input variable.

In this case....

$x = \text{input} = \text{independent variable} = \text{domain}$

$y = \text{output} = \text{dependent variable} = \text{range}$

$f(x)$  does not mean multiply  $f$  by  $x$  !!!!!!!!!!!

Linear Equations:  $y = mx + b$

Linear Functions:  $f(x) = mx + b$

Function  
Notation

$f(x)$  means the output value of the function when the input value is the number  $x$ .

For example  $f(8)$  means the value of the function evaluated for an input value of 8.

For  $f(x)$  we say, "f of x." For  $f(8)$ , we say, "f of 8."

$$y = 3x - 5$$

$$f(x) = 3x - 5$$

$$f(8) = 3(8) - 5$$

$$f(8) = 19$$